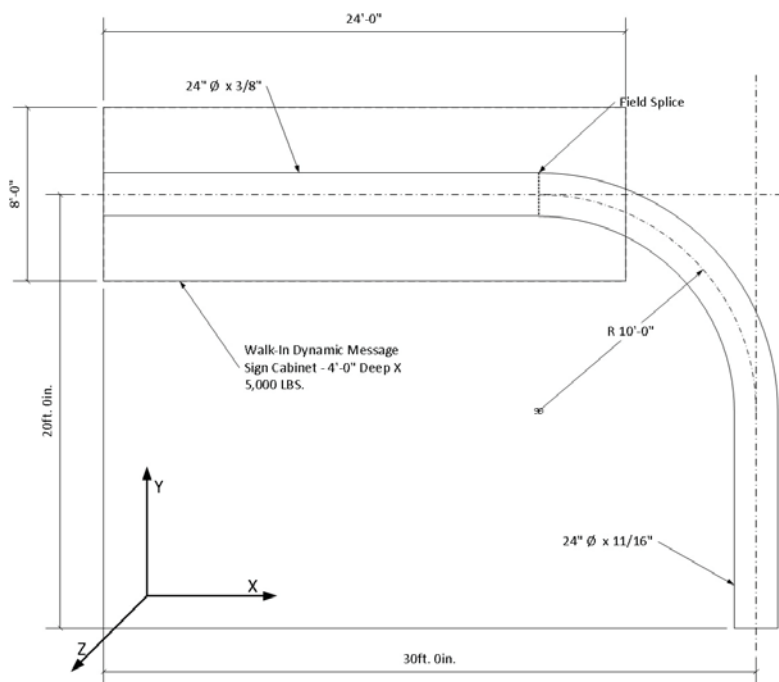


## Design Example 9

### Cantilevered Monotube Support for a Dynamic Message Sign

#### Problem Statement:

Design a cantilevered monotube structure in Ft. Collins, CO. It will support a dynamic message sign weighing 5,000 pounds. Assume a 24" diameter circular tube fabricated from A36 steel. Bolts are ASTM A 325 bolts. The structure would cross a lifeline travelway on failure.



➤ Reference:E:\BT\Projects\NCHRP 10-80\Examples\Release\SpecificationFunctions.xmcd(R)

Several commonly-used functions are stored in a separate include file that is used in multiple example problems. These include functions to determine  $C_d$  and resistance values for flexure, shear, and torsion for common steel shapes. You may need to reset the path to this file for your computer by right-clicking on the reference.

☐ Contents

[Definitions and Assumptions](#)

[Dead Loads](#)

[Wind Loads](#)

[Factored Actions](#)

[Resistance at the Tube Splice](#)

[Resistance at the Post Base](#)

[Base Plate Design](#)

[Fatigue Limits](#)

[Fatigue - Natural Wind Gusts](#)

[Fatigue - Truck Gusts](#)

⬆ Contents

☐ Definitions And Assumptions

**Definitions and Assumptions:**

[Back to Contents](#)

Materials:

$t_{ice} := 0.25\text{in}$

$\gamma_{steel} := 490 \frac{\text{lbf}}{\text{ft}^3}$

$\gamma_{ice} := 56.8 \frac{\text{lbf}}{\text{ft}^3}$

$$F_y := 36\text{ksi}$$

$$E_s := 29000\text{ksi}$$

$$l_{\text{total}} := 30\text{ft}$$

Total sign length

$$h_{\text{total}} := 20\text{ft}$$

Height to the centerline of the tube

Sign:

$$b_{\text{sign}} := 24\text{ft}$$

$$h_{\text{sign}} := 8\text{ft}$$

$$d_{\text{sign}} := 4\text{ft}$$

$$P_{\text{sign}} := 5\text{kip}$$

$$EPA_{\text{sign}_x} := 32\text{ft}^2$$

$$\text{BendRadius} := 10\text{ft}$$

Wind Loads:

**Table 3.8-1—Mean Recurrence Interval**

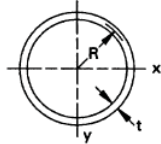
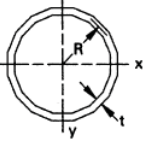
Traffic Volume	Risk Category		
	Typical	High	Low
ADT<100	300	1700	300
100<ADT≤1000	700	1700	300
1000<ADT≤10000	700	1700	300
ADT>10000	1700	1700	300
Typical: Failure could cross travelway			
High: Support failure could stop a lifeline travelway			
Low: Support failure could not cross travelway			
Roadside sign supports: use 300 years			

MRI is 1700, therefore use Figure 3.8-2a

$$V_{E1} := 120\text{mph}$$

Figure 3.8-2a

Table B1-1—Estimated Sectional Properties for Common Tubular Shapes

Property	Round Tube	Hexdecagonal Tube
Moment of inertia, $I$	$3.14R^3t$	$3.22R^3t$
Section modulus, $S$	$3.14R^2t$	$3.22R^2t$
Area, $A$	$6.28Rt$	$6.37Rt$
Shape factor, $K_p = Z/S$	1.27	1.27
Radius of gyration, $r$	$0.707R$	$0.711R$
Cross-sectional constant, $C$	3.14	3.22
Pictorial representation		

Tubes:

The bottom tube is 24" diameter,  $t = 11/16$ "

$$d_{\text{bot}} := 24\text{in}$$

$$t_{\text{bot}} := \frac{11}{16}\text{in}$$

$$r_{\text{bend}} := 10\text{ft} \quad \text{Bend radius of the tube.}$$

$$d_{\text{bot\_out}} := d_{\text{bot}} + t_{\text{bot}} = 24.7\text{in}$$

$$d_{\text{bot\_in}} := d_{\text{bot}} - t_{\text{bot}} = 23.3\text{in}$$

$$I := \pi \cdot \left( \frac{d_{\text{bot}}}{2} \right)^3 t_{\text{bot}} = 3732 \cdot \text{in}^4$$

$$A_{\text{bot}} := \pi \cdot \frac{(d_{\text{bot\_out}}^2 - d_{\text{bot\_in}}^2)}{4} = 51.8 \cdot \text{in}^2$$

$$I_{\text{bot}} := \pi \cdot \frac{(d_{\text{bot\_out}}^4 - d_{\text{bot\_in}}^4)}{64} = 3735 \cdot \text{in}^4$$

$$S_{\text{bot}} := \pi \cdot \frac{(d_{\text{bot\_out}}^4 - d_{\text{bot\_in}}^4)}{32 \cdot d_{\text{bot\_out}}} = 303 \cdot \text{in}^3$$

$$r_{\text{gybot}} := \frac{\sqrt{d_{\text{bot\_out}}^2 + d_{\text{bot\_in}}^2}}{4} = 8.49\text{in}$$

The top tube is 24" diameter, t = 3/8"

$$d_{\text{top}} := 24 \text{ in} \quad t_{\text{top}} := \frac{3}{8} \text{ in}$$

$$d_{\text{top\_out}} := d_{\text{top}} + t_{\text{top}} = 24.4 \text{ in}$$

$$d_{\text{top\_in}} := d_{\text{top}} - t_{\text{top}} = 23.6 \text{ in}$$

$$A_{\text{top}} := \pi \cdot \frac{(d_{\text{top\_out}}^2 - d_{\text{top\_in}}^2)}{4} = 28.3 \cdot \text{in}^2$$

$$I_{\text{top}} := \pi \cdot \frac{(d_{\text{top\_out}}^4 - d_{\text{top\_in}}^4)}{64} = 2036 \cdot \text{in}^4$$

$$S_{\text{top}} := \pi \cdot \frac{(d_{\text{top\_out}}^4 - d_{\text{top\_in}}^4)}{32 \cdot d_{\text{top\_out}}} = 167 \cdot \text{in}^3$$

$$r_{\text{gytop}} := \frac{\sqrt{d_{\text{top\_out}}^2 + d_{\text{top\_in}}^2}}{4} = 8.49 \cdot \text{in}$$

$$l_{\text{top}} := 14 \text{ ft} \quad l_{\text{bot}} := \frac{\pi \cdot 2 \cdot r_{\text{bend}}}{4} + 10 \text{ ft} = 25.7 \text{ ft}$$

## Load Factors:

Table 3.4-1--- Load Combinations and Load Factors

Load Combination Limit State	Description	Reference Articles	Permanent		Transient			Fatigue			
			Dead Components (DC)		Live Load (LL)	Wind (W)	Truck Gust (TrG)	Natural Wind Gust Vibration (NWG)	Vortex-Induced Vibration (VIV)	Combined Wind on High-level Towers	Galloping Induced Vibration (GVW)
			Max/Min	Mean				Apply separately			
Strength I	Gravity	3.5, 3.6, and 3.7	1.25		1.6						
Extreme I	Wind	3.5, 3.8, 3.9	1.1/0.9			1.0 <sup>a</sup>					
Service I	Translation	10.4		1.0		1.0 <sup>b</sup>					
Service III	Crack control for Prestressed Concrete			1.0		1.00					
Fatigue I	Infinite-life	11.7		1.0			1.0	1.0	1.0	1.0	1.0
Fatigue II	Evaluation	17.5		1.0			1.0	1.0	1.0	1.0	1.0

a. Use Figures 3.8-1, 3.8-2, or 3.8-3 (for appropriate return period)

b. Use wind map 3.8-4 (service)

## Resistance Factors:

$$\phi_{\text{flexure}} := 0.90 \quad \phi_{\text{shear}} := 0.90 \quad \phi_{\text{weld}} := 0.75 \quad \phi_{\text{torsion}} := 0.95 \quad \phi_{\text{axial}} := 0.90 \quad \text{Article 5.5.3.2}$$

$$\phi_{\text{bolt\_tension}} := 0.75 \quad \phi_{\text{bolt\_shear}} := 0.33$$

## Load Factors:

$$\gamma_{\text{DC\_E1}} := 1.1 \quad \gamma_{\text{W\_E1}} := 1.0$$

## Dead Loads

[Back to Contents](#)

$$P_{\text{sign}} = 5.00 \cdot \text{kip}$$

$$d_{z\_sign} := l_{\text{total}} - \frac{b_{\text{sign}}}{2} = 18.0 \text{ ft}$$

Tube weights:

$$P_{\text{tube\_top}} := A_{\text{top}} \cdot \gamma_{\text{steel}} \cdot l_{\text{top}} = 1.35 \cdot \text{kip}$$

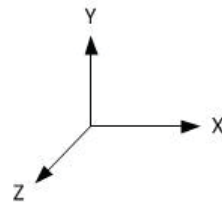
$$P_{\text{tube\_bot}} := A_{\text{bot}} \cdot \gamma_{\text{steel}} \cdot l_{\text{bot}} = 4.53 \cdot \text{kip}$$

$$P_{\text{tube\_tot}} := P_{\text{tube\_top}} + P_{\text{tube\_bot}} = 5.88 \cdot \text{kip}$$

Tube moment arms:

$$d_{z\_top\_tube} := r_{\text{bend}} + \frac{l_{\text{top}}}{2} = 17.0 \text{ ft}$$

$$d_{z\_bot\_tube} := \frac{r_{\text{bend}} \text{ ft} \cdot 0 + (l_{\text{bot}} - r_{\text{bend}}) \cdot \frac{4r_{\text{bend}}}{3 \cdot \pi}}{l_{\text{bot}}} = 2.59 \text{ ft}$$



Distance from the centerline of the bottom of the tube to the centroid of the straight and bent tube.

Moments at the base:

$$M_{z\_DC\text{Sign}} := P_{\text{sign}} \cdot d_{z\_sign} = 90.0 \cdot \text{kip} \cdot \text{ft}$$

$$M_{z\_DC\text{Tube}} := d_{z\_top\_tube} \cdot P_{\text{tube\_top}} + d_{z\_bot\_tube} \cdot P_{\text{tube\_bot}} = 34.7 \cdot \text{kip} \cdot \text{ft}$$

Moments at the field splice:

$$M_{Z\_DCSign\_splice} := P_{sign} \cdot \frac{l_{top}}{2} = 35.0 \cdot \text{kip} \cdot \text{ft}$$

$$M_{Z\_DCTube\_splice} := P_{tube\_top} \cdot \frac{l_{top}}{2} = 9.43 \cdot \text{kip} \cdot \text{ft}$$

$$V_{DC\_sign\_splice} := P_{sign} = 5.00 \cdot \text{kip}$$

$$V_{DC\_tube\_splice} := P_{tube\_top} = 1.35 \cdot \text{kip}$$

▢ Dead Loads

---

▼ Wind Loads

---

### **Wind Loads**

[Back to Contents](#)

**Areas:**

$$A_{sign} := b_{sign} \cdot h_{sign} = 192 \text{ ft}^2 \quad EPA_{sign\_x} = 32 \text{ ft}^2$$

Assume the tube is exposed all the way to the field splice.

$$A_{tube\_vert} := (h_{total} - r_{bend}) \cdot d_{bot\_out} = 20.6 \text{ ft}^2$$

Area of the tube perpendicular to the z axis

$$A_{tube\_bend} := \left( \frac{2 \cdot \pi \cdot r_{bend}}{4} \right) \cdot d_{bot\_out} = 32.3 \text{ ft}^2$$

$$A_{tube} := A_{tube\_vert} + A_{tube\_bend} = 52.9 \text{ ft}^2$$

$$A_{tube\_x} := h_{total} \cdot d_{bot\_out} = 41 \text{ ft}^2$$

Area of the tube perpendicular to the x axis



**Pressures:**

$$z := h_{\text{total}} = 20 \text{ ft}$$

Height above ground for pressure calculation. C3.8.4.

$$z_g := 900 \text{ ft}$$

Constant based on exposure condition. C3.8.4.

$$\alpha := 9.5$$

Constant based on exposure condition. C3.8.4.

$$\text{Factor} := \frac{\text{hr}^2 \cdot \text{lbf}}{27878400 \cdot \text{ft}^4}$$

This units factor is needed for consistent units in the wind pressure equations.

$$K_z := 2.00 \left( \frac{z}{z_g} \right)^{\frac{2}{\alpha}} = 1$$

Equation 3.8.4-1

$$G := 1.14$$

Gust effect factor, minimum value.

$$V_{E1} = 120 \cdot \text{mph}$$

Extreme I Wind Speed - Figure 3.8-2b, 1700 year mean recurrence interval.

$K_{d\_tube} := 0.95$

$K_{d\_sign} := 0.85$

Directionality factor, see 3.8.5 for a round support.

Directionality factor, see 3.8.5 for a Dynamic Message Sign.

**Table 3.8.5-1—Directionality Factors,  $K_d$**

Support Type	Directionality Factor
High-mast and Pole	
Round	0.95
Square	0.9
Octagonal	0.95
Dodecagonal	0.95
Hexdecagonal	0.95
Traffic Signal	0.85
Dynamic Message Sign	0.85
Overhead Frame/Truss	0.85
Support with horizontal arms or members supporting sign and/or signals	0.85

Tube:

$$C_{d\_tube\_E1} := C_{d\_cylindrical}(V_{E1}, d_{bot\_out}) = 0.45$$

$$P_{z\_tube\_E1} := 0.00256 \cdot K_z \cdot K_{d\_tube} \cdot G \cdot V_{E1}^2 \cdot C_{d\_tube\_E1} \cdot Factor = 16.1 \cdot psf$$

$$P_{tube\_E1} := P_{z\_tube\_E1} \cdot A_{tube} = 0.85 \cdot kip$$

Causes moment about the x axis

$$P_{tube\_E1\_z} := P_{z\_tube\_E1} \cdot A_{tube\_x} = 0.663 \cdot kip$$

Causes moment about the y axis (torsion at the base plate).

$$M_{x\_E1} := P_{tube\_E1} \cdot d_{z\_bot\_tube} = 2.21 \cdot kip \cdot ft$$

$$M_{y\_E1} := P_{tube\_E1\_z} \cdot \frac{h_{total}}{2} = 6.63 \cdot kip \cdot ft$$

Sign:

$$C_{dSign} := C_{d\_sign} \left( \frac{b_{sign}}{h_{sign}} \right) = 1$$

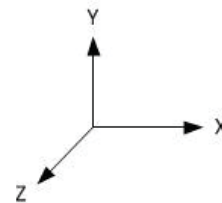
$$P_{z\_sign\_E1} := 0.00256 \cdot K_z \cdot K_{d\_sign} \cdot G \cdot V_{E1}^2 \cdot C_{dSign} \cdot Factor = 38.1 \cdot psf$$

$$P_{sign\_E1} := P_{z\_sign\_E1} \cdot A_{sign} = 7.32 \cdot kip$$

$$M_{x\_sign\_E1} := P_{sign\_E1} \cdot h_{total} = 146 \cdot kip \cdot ft$$

$$M_{y\_sign\_E1} := P_{sign\_E1} \cdot d_{z\_sign} = 132 \cdot kip \cdot ft$$

Torsion at the base of the tube.



## Factored Actions

[Back to Contents](#)

### Resistance Factors:

$$\phi_{\text{flexure}} = 0.90 \quad \phi_{\text{shear}} = 0.90 \quad \phi_{\text{weld}} = 0.75 \quad \phi_{\text{torsion}} = 0.95 \quad \phi_{\text{axial}} = 0.90$$

$$\gamma_{\text{DC\_E1}} = 1.10 \quad \gamma_{\text{W\_E1}} = 1.00$$

### Extreme Event I, Maximum Wind plus Dead

Actions at the field splice:

Assume that all the moment from the sign is carried by the field splice.

$$M_{\text{Z\_DCSign\_splice}} = 35.0 \cdot \text{kip} \cdot \text{ft} \quad M_{\text{Z\_DCTube\_splice}} = 9.43 \cdot \text{kip} \cdot \text{ft}$$

$$V_{\text{DC\_sign\_splice}} = 5.00 \cdot \text{kip} \quad V_{\text{DC\_tube\_splice}} = 1.347 \cdot \text{kip}$$

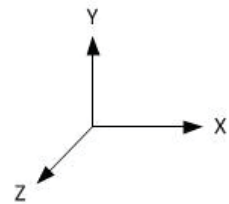
$$M_{\text{splice\_E1}} := \sqrt{\left[ \gamma_{\text{DC\_E1}} \cdot (M_{\text{Z\_DCSign\_splice}} + M_{\text{Z\_DCTube\_splice}}) \right]^2 + \left( \gamma_{\text{W\_E1}} \cdot P_{\text{sign\_E1}} \cdot \frac{l_{\text{top}}}{2} \right)^2} = 70.8 \cdot \text{kip} \cdot \text{ft}$$

$$V_{\text{splice\_E1}} := \sqrt{\left[ \gamma_{\text{DC\_E1}} \cdot (V_{\text{DC\_sign\_splice}} + V_{\text{DC\_tube\_splice}}) \right]^2 + \left( \gamma_{\text{W\_E1}} \cdot P_{\text{sign\_E1}} \right)^2} = 10.1 \cdot \text{kip}$$

Actions at the tube base:

$$M_{\text{x\_sign\_E1}} = 146 \cdot \text{kip} \cdot \text{ft} \quad M_{\text{Z\_DCSign}} = 90 \cdot \text{kip} \cdot \text{ft} \quad M_{\text{Z\_DCTube}} = 34.7 \cdot \text{kip} \cdot \text{ft}$$

$$M_{\text{y\_sign\_E1}} = 132 \cdot \text{kip} \cdot \text{ft}$$



$$P_{\text{sign\_E1}} = 7.32 \cdot \text{kip}$$

$$M_{\text{tube\_E1}} := \sqrt{\left[ \gamma_{\text{DC\_E1}} \cdot (M_{\text{Z\_DCSign}} + M_{\text{Z\_DCTube}}) \right]^2 + \left( \gamma_{\text{W\_E1}} \cdot M_{\text{x\_sign\_E1}} \right)^2} = 201 \cdot \text{kip} \cdot \text{ft}$$

$$T_{\text{tube\_E1}} := \gamma_{\text{W\_E1}} \cdot M_{\text{y\_sign\_E1}} = 132 \cdot \text{kip} \cdot \text{ft} \quad \text{torsion}$$

$$V_{\text{tube\_E1}} := \gamma_{\text{W\_E1}} \cdot (P_{\text{sign\_E1}} + P_{\text{tube\_E1}}) = 8.18 \cdot \text{kip}$$

$$P_{\text{u\_tube}} := \gamma_{\text{DC\_E1}} \cdot (P_{\text{sign}} + P_{\text{tube\_tot}}) = 12.0 \cdot \text{kip}$$

▣ Factored Loads

▣ Resistance at the Tube Splice

### **Resistances at the Splice**

[Back to Contents](#)

$$A_{\text{shear\_splice}} := \frac{A_{\text{top}}}{2} = 14.14 \cdot \text{in}^2 \quad d_{\text{top}} = 24 \cdot \text{in} \quad t_{\text{top}} = 0.375 \cdot \text{in}$$

$$Z_{\text{top}} := \frac{d_{\text{top\_out}}^3}{6} - \frac{d_{\text{top\_in}}^3}{6} = 216 \cdot \text{in}^3$$

$$L_{\text{v\_splice}} := l_{\text{top}} = 14 \cdot \text{ft}$$

$$L_{\text{t\_splice}} := \pi \cdot d_{\text{top}} = 75 \cdot \text{in}$$

$$V_{\text{n}} := V_{\text{n\_roundTube}}(A_{\text{shear\_splice}}, d_{\text{top}}, t_{\text{top}}, E_{\text{s}}, F_{\text{y}}, L_{\text{v\_splice}}) = 305 \cdot \text{kip}$$

$$J_{\text{top}} := 2 \cdot I_{\text{top}} = 4072 \cdot \text{in}^4$$

$$F_{\text{nt}} := F_{\text{nt\_roundTube}}(F_{\text{v}}, E_{\text{s}}, d_{\text{top}}, t_{\text{top}}, L_{\text{v\_splice}}) = 21.60 \cdot \text{ksi}$$

$$T_{\text{n}} := A_{\text{top}} \cdot F_{\text{nt}} \left( \frac{d_{\text{top}}}{2} \right) = 610.7 \cdot \text{ft} \cdot \text{kip}$$

$$M_n := M_{n\_roundTube}(d_{top}, t_{top}, E_s, F_y, Z_{top}, S_{top}) = 630 \cdot \text{kip} \cdot \text{ft}$$

$$M_{splice\_E1} = 70.8 \cdot \text{kip} \cdot \text{ft}$$

$$V_{splice\_E1} = 10.12 \cdot \text{kip}$$

$$T_{tube\_E1} = 131.8 \cdot \text{kip} \cdot \text{ft}$$

$$\text{InteractionValue} := \left( \frac{M_{splice\_E1}}{\phi_{flexure} \cdot M_n} \right) + \left( \frac{V_{splice\_E1}}{\phi_{shear} \cdot V_n} + \frac{T_{tube\_E1}}{\phi_{torsion} \cdot T_n} \right)^2 = 0.19$$

$$\text{InteractionCheck}_{splice\_E1} := \text{if}(\text{InteractionValue} \leq 1.0, \text{"OK"}, \text{"No Good"}) = \text{"OK"}$$

▢ Resistance at the Tube Splice

▼ Resistance at the Tube Base

### Resistances at the Base

[Back to Contents](#)

$$A_{shear\_base} := \frac{A_{bot}}{2} = 25.9 \cdot \text{in}^2 \quad d_{bot} = 24 \cdot \text{in} \quad t_{bot} = 0.688 \cdot \text{in}$$

$$Z_{bot} := \frac{d_{bot\_out}^3}{6} - \frac{d_{bot\_in}^3}{6} = 396 \cdot \text{in}^3$$

$$k_{tube} := 2.1 \quad r_{gytube} := 0.707 \cdot \frac{d_{bot}}{2} = 8.48 \cdot \text{in}$$

$$kl\_over\_r_{tube} := \frac{k_{tube} \cdot l_{total}}{r_{gytube}} = 89.1$$

$$L_{v\_base} := l_{total} = 30 \cdot \text{ft}$$

$$L_{t\_base} := \pi \cdot d_{bot} = 75 \cdot \text{in}$$

$$Q := 1.0$$

$$V_n := V_{n\_roundTube}(A_{shear\_base}, d_{bot}, t_{bot}, E_s, F_y, L_{v\_base}) = 307 \cdot \text{kip}$$

$$I_{top} := 2 \cdot I_{top} = 4072 \cdot \text{in}^4$$

$$F_{nt} := F_{nt\_roundTube}(F_y, E_s, d_{bot}, t_{bot}, L_{v\_base}) = 21.6 \cdot \text{ksi}$$

$$T_n := A_{bot} \cdot F_{nt} \cdot \frac{d_{bot}}{2} = 1120 \cdot \text{ft} \cdot \text{kip}$$

$$M_n := M_{n\_roundTube}(d_{top}, t_{top}, E_s, F_y, Z_{top}, S_{top}) = 630 \cdot \text{kip} \cdot \text{ft}$$

$$P_n := P_{n\_roundTube}(A_{bot}, F_y, k_l\_over\_r_{tube}, E_s, Q) = 1229 \cdot \text{kip}$$

$$M_{tube\_E1} = 201 \cdot \text{kip} \cdot \text{ft}$$

$$V_{tube\_E1} = 8 \cdot \text{kip}$$

$$P_{u\_tube} = 11.97 \cdot \text{kip}$$

$$T_{tube\_E1} = 132 \cdot \text{kip} \cdot \text{ft}$$

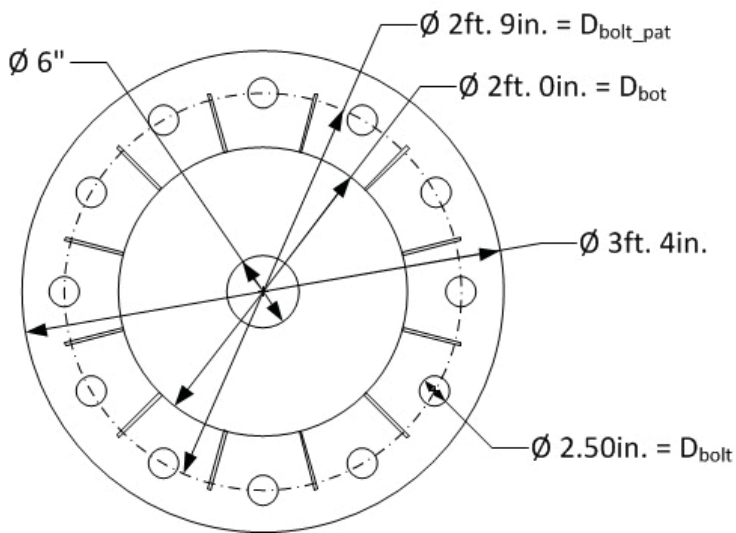
$$\frac{P_{u\_tube}}{P_n} = 0.010 \quad \frac{T_{tube\_E1}}{T_n} = 0.118$$

$$InteractionValue := \left( \frac{M_{tube\_E1}}{\phi_{flexure} \cdot M_n} \right) + \left( \frac{V_{tube\_E1}}{\phi_{shear} \cdot V_n} + \frac{T_{tube\_E1}}{\phi_{torsion} \cdot T_n} \right)^2 = 0.38$$

$$InteractionCheck_{splice\_E1} := \text{if}(InteractionValue \leq 1.0, "OK", "No Good") = "OK"$$

## Base Plate Design

[Back to Contents](#)



$$t_{\text{min}} := 2\text{in}$$

Minimum base plate thickness, 5.6.3.

Bolts:

$$\phi_{\text{bolt\_tension}} = 0.75$$

$$\phi_{\text{bolt\_shear}} = 0.33$$

$$n_{\text{bolts}} := 12$$

$$F_{y\_bolts} := 55\text{ksi}$$

$$F_{u\_bolts} := 70\text{ksi}$$

$$D_{\text{bolt}} := 1.00\text{in}$$



$$A_{\text{bolt}} := \frac{\pi}{4} \cdot (D_{\text{bolt}})^2 = 0.79 \cdot \text{in}^2$$

$$D_{\text{bolt\_pat}} := 33.0 \text{ in}$$

See figure above for geometry.

$$C_{\text{bolts}} := \frac{D_{\text{bolt\_pat}}}{2} = 17 \cdot \text{in}$$

$$I_1 := A_{\text{bolt}} \cdot C_{\text{bolts}}^2 = 214 \cdot \text{in}^4$$

$$I_2 := A_{\text{bolt}} \cdot (C_{\text{bolts}} \cdot \sin(60\text{deg}))^2 \cdot 2 = 321 \cdot \text{in}^4$$

$$I_3 := A_{\text{bolt}} \cdot (C_{\text{bolts}} \cdot \sin(30\text{deg}))^2 \cdot 2 = 107 \cdot \text{in}^4$$

$$I_{\text{bolts}} := 2 \cdot (I_1 + I_2 + I_3) = 1283 \cdot \text{in}^4$$

Tension in bolts, Extreme Event I:

$$P_{u\_bolt} := \left( \frac{M_{\text{tube\_E1}} \cdot C_{\text{bolts}}}{I_{\text{bolts}}} \right) \cdot A_{\text{bolt}} = 24.3 \cdot \text{kip}$$

Shear in bolts, Extreme Event I:

$$V_{u\_bolt} := \frac{V_{\text{tube\_E1}}}{n_{\text{bolts}}} = 0.68 \cdot \text{kip}$$

Shear in bolts from torsion, Extreme Event I:

$$T_{u\_bolt} := \frac{T_{\text{tube\_E1}}}{D_{\text{bolt\_pat}} \cdot n_{\text{bolts}}} = 4.00 \cdot \text{kip}$$

Total Shear:

$$V_{u\_bolt} := V_{u\_bolt} + T_{u\_bolt} = 4.68 \cdot \text{kip}$$

Bolt Resistances:

$$P_{n\_bolt} := \phi_{bolt\_tension} \cdot F_{u\_bolts} \cdot A_{bolt} = 41.2 \cdot \text{kip}$$

$$V_{n\_bolt} := \phi_{bolt\_shear} \cdot F_{u\_bolts} \cdot A_{bolt} = 18.1 \cdot \text{kip}$$

Combined Bolt Resistance:

$$\text{InteractionValue}_{bolts} := \left( \frac{P_{u\_bolt}}{P_{n\_bolt}} \right)^2 + \left( \frac{V_{u\_bolt}}{V_{n\_bolt}} \right)^2 = 0.414$$

$$\text{InteractionCheck}_{bolts} := \text{if} \left( \text{InteractionValue}_{bolts} \leq 1.0, "OK", "No Good" \right) = "OK"$$

$$F_{y\_bp} := 36 \text{ksi}$$

Calculate an eccentricity equal to half the distance from the center of the bolt to the toe of the weld. Assume a weld size.

$$t_{\text{weld}} := 0.50 \text{ in}$$

$$d_{\text{bolt}} := \left( \frac{D_{\text{bolt\_pat}} - d_{\text{bot}}}{2} \right) = 4.50 \cdot \text{in}$$

$$d_{\text{weld\_bolt}} := \frac{D_{\text{bolt\_pat}}}{2} - t_{\text{weld}} = 16.00 \cdot \text{in}$$

$$e_{\text{bp}} := \frac{d_{\text{weld\_bolt}}}{2} = 8 \cdot \text{in}$$

$$M_{\text{bp}} := P_{\text{u\_bolt}} \cdot e_{\text{bp}} = 16.21 \cdot \text{kip} \cdot \text{ft}$$

$$\theta_{\text{bolt}} := \frac{360 \text{ deg}}{n_{\text{bolts}}} = 30 \cdot \text{deg}$$

Each bolt covers an arc of 30 degrees

$$d_e := \frac{d_{\text{bot}} + t_{\text{weld}} + e_{\text{bp}}}{2} = 16.25 \cdot \text{in}$$

$$b_{\text{bp\_section}} := 2 \cdot \text{atan} \left( \frac{\theta_{\text{bolt}}}{2} \right) \cdot d_e = 8.32 \cdot \text{in}$$

The width of a 30 degree arc at the location of eccentricity

$$t_{\text{min}} = 2 \cdot \text{in}$$

$$Z_{\text{bp}} := \frac{b_{\text{bp\_section}} \cdot t_{\text{min}}^2}{4} = 8.32 \cdot \text{in}^3$$

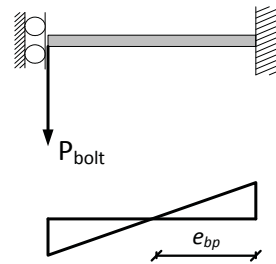
Table 5.6.3-1

$$M_{\text{n\_bp}} := F_{\text{y\_bp}} \cdot Z_{\text{bp}} = 25 \cdot \text{kip} \cdot \text{ft}$$

$$\text{ratio}_{\text{bp}} := \frac{M_{\text{bp}}}{\phi_{\text{flexure}} \cdot M_{\text{n\_bp}}} = 0.72$$

$$\text{InteractionCheck}_{\text{bp}} := \text{if} \left( \text{ratio}_{\text{bp}} \leq 1.0, \text{"OK"}, \text{"No Good"} \right) = \text{"OK"}$$

Distance from the face of the tube to the center of a bolt.



Moment Diagram in Base Plate

## Weld Design

[Back to Contents](#)

$$\phi_{\text{weld}} = 1 \quad F_{\text{EXX}} := 70 \text{ ksi} \quad F_{\text{n\_weld}} := 0.60 \cdot F_{\text{EXX}} = 42 \cdot \text{ksi}$$

$$M_{\text{tube\_E1}} = 201 \cdot \text{kip} \cdot \text{ft} \quad V_{\text{tube\_E1}} = 8 \cdot \text{kip}$$

$$t_{\text{weld}} = 0.5 \cdot \text{in}$$

$$\text{radius}_{\text{bot}} := \frac{d_{\text{bot}}}{2} = 12 \cdot \text{in}$$

$$S_{\text{weld}} := \pi \cdot \text{radius}_{\text{bot}}^2 = 452 \cdot \text{in}^2$$

$$V_{\text{u\_weld}} := \sqrt{\left( \frac{M_{\text{tube\_E1}}}{S_{\text{weld}}} \right)^2 + \left( \frac{V_{\text{tube\_E1}}}{2 \cdot \pi \cdot \text{radius}_{\text{bot}}} \right)^2} = 5.32 \cdot \frac{\text{kip}}{\text{in}}$$

$$V_{\text{n\_weld}} := t_{\text{weld}} \cdot F_{\text{n\_weld}} = 21.0 \cdot \frac{\text{kip}}{\text{in}}$$

$$\text{ratio}_{\text{weld}} := \frac{V_{\text{u\_weld}}}{\phi_{\text{weld}} \cdot V_{\text{n\_weld}}} = 0.34$$

$$\text{WeldCheck} := \text{if}(\text{ratio}_{\text{weld}} < 1.00, \text{"OK"}, \text{"No Good"})$$

The 1/2" weld supplies adequate capacity.

Section modulus of the outer weld pattern.

Resultant shear on the weld.

Factored resistance of the outer weld.

WeldCheck = "OK"

### ***Fatigue Limits***

[Back to contents](#)

$$D_T := d_{\text{bot}} = 24.0 \cdot \text{in}$$

External diameter of a round tube.

$$D_{BC} := D_{\text{bolt\_pat}} = 33.0 \cdot \text{in}$$

Diameter of a circle through the fasteners in the transverse plate.

$$N_B := 12$$

Number of fasteners in the transverse plate.

$$t_T := t_{\text{bot}} = 0.6875 \cdot \text{in}$$

Thickness of the tube.

$$t_{TP} := t_{\text{min}} = 2.00 \cdot \text{in}$$

Thickness of the transverse plate.

$$D_{OP} := 4 \cdot \text{in}$$

Diameter of the concentric opening in the transverse plate.  
Assume a value.

$$C_{OP} := \frac{D_{OP}}{D_T} = 0.17$$

$$C_{BC} := \frac{D_{BC}}{D_T} = 1.38$$

$$t_{ST} := 0$$

Stiffener thickness, not applicable for this case

$$N_{ST} := 0$$

Number of stiffeners, NA

$$h_{ST} := 0$$

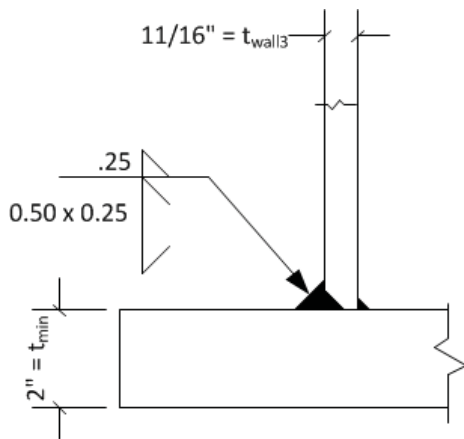
Height of stiffeners, NA

$$N_S := 1$$

Number of sides for multi-sided tube, NA

$$r_b := 0$$

Inside bend radius, use 0 for a round tube



4.6 Full penetration groove-welded tube-to-transverse plate connections welded from both sides with back-gouging (without backing ring). From Table 11.9.3.1-1.

Groove-welded tube-to-transverse plate connections: Section type for equation 11.9.3.1-13. From Table 11.9.3.1-2.

$$K_{F\_pole} := K_F(13, D_T, D_{BC}, N_B, t_T, t_{TP}, D_{OP}, t_{ST}, N_{ST}, h_{ST}, N_S, r_b) = 1.85 \quad \text{See included sheet.}$$

$$K_{I\_pole} := \left[ \left( 1.76 + 1.83 \cdot \frac{t_T}{\text{in}} \right) - 4.76 \cdot 0.22^{K_{F\_pole}} \right] \cdot K_{F\_pole} = 5.04 \quad \text{Equation 11.9.3.1-1}$$

$$\Delta F_{TH\_weld} := \Delta F(K_{I\_pole}) = 7.0 \cdot \text{ksi}$$

$$\Delta F_{TH\_bolts} := 7.0 \text{ ksi} \quad \text{See Table 11.9.3.1-1, 2.3}$$

### Natural Wind Gusts (11.7.1.2):

[Back to contents](#)

The maximum yearly mean wind velocity of National Weather Stations in Ft. Collins, CO is 11.2 mph.

C11.6 states the cantilevers supporting variable message may be classified as fatigue category 1.

$$I_F := 1.0$$

Table 11.6-1

$$C_{d\text{Sign}} = 1.19$$

$$V_{\text{mean}} := 11.2 \text{ mph}$$

$$C_{d\_pole} := C_{d\_cylindrical}(V_{\text{mean}}, d_{\text{top}}) = 1.10$$

Table 3.8.7-1 Different arm Cd due to lower wind speed.

$$P_{\text{NW\_pole}} := 5.2 \frac{\text{lbf}}{\text{ft}^2} \cdot C_{d\_pole} \cdot I_F = 5.72 \cdot \text{psf}$$

Equation C11.7.1.2-1

$$P_{\text{NW\_sign}} := 5.2 \frac{\text{lbf}}{\text{ft}^2} \cdot C_{d\text{Sign}} \cdot I_F = 6.19 \cdot \text{psf}$$

$$P_{\text{NW\_pole}} := P_{\text{NW\_pole}} \cdot (A_{\text{tube}}) = 0.303 \cdot \text{kip}$$

Wind force times the area of pole exposed.

$$P_{\text{NW\_sign}} := P_{\text{NW\_sign}} \cdot (A_{\text{sign}}) = 1.188 \cdot \text{kip}$$

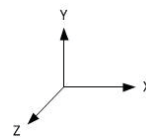
Wind force times the area of the sign.

$$P_{\text{NW\_total}} := P_{\text{NW\_pole}} + P_{\text{NW\_sign}}$$

$$M_{\text{xNW\_pole}} := P_{\text{NW\_pole}} \cdot h_{\text{total}} = 6.05 \cdot \text{kip} \cdot \text{ft}$$

$$M_{\text{xNW\_sign}} := P_{\text{NW\_sign}} \cdot h_{\text{total}} = 23.8 \cdot \text{kip} \cdot \text{ft}$$

$$M_{\text{xNW\_total}} := M_{\text{xNW\_pole}} + M_{\text{xNW\_sign}} = 29.8 \cdot \text{kip} \cdot \text{ft}$$



$$\sigma_{\text{NW\_weld}} := \frac{M_{\text{xNW\_total}} \cdot \frac{d_{\text{bot}}}{2}}{I_{\text{bot}}} = 1.149 \cdot \text{ksi}$$

$$\text{ratio}_{\text{NW}} := \frac{\sigma_{\text{NW\_weld}}}{\Delta F_{\text{TH\_weld}}} = 0.16$$

$$\text{CheckWeld}_{\text{NW}} := \text{if} \left( \text{ratio}_{\text{NW}} \leq 1.0, \text{"OK"}, \text{"No Good"} \right) = \text{"OK"}$$

▣ Natural Wind Gusts

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▣ Truck Gusts

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### Truck Gusts (11.7.1.3):

[Back to contents](#)

$$b_{\text{sign}} = 24 \text{ ft} \quad d_{\text{sign}} = 4 \text{ ft}$$

$$C_{\text{dSign\_vertical}} := C_{\text{d\_sign}} \left( \frac{b_{\text{sign}}}{d_{\text{sign}}} \right) = 1.2$$

$$P_{\text{TG\_sign}} := 18.8 \text{ psf} \cdot C_{\text{dSign\_vertical}} \cdot I_{\text{F}} = 22.6 \cdot \text{psf}$$

$$P_{\text{TG\_pole}} := 18.8 \text{ psf} \cdot C_{\text{d\_pole}} \cdot I_{\text{F}} = 20.7 \cdot \text{psf}$$

$$P_{\text{TG\_sign}} := P_{\text{TG\_sign}} \cdot (b_{\text{sign}} \cdot d_{\text{sign}}) = 2.17 \cdot \text{kip}$$

$$P_{\text{TG\_pole}} := P_{\text{TG\_pole}} \cdot (l_{\text{total}} \cdot d_{\text{top}}) = 1.24 \cdot \text{kip}$$

$$M_{\text{zTG\_sign}} := P_{\text{TG\_sign}} \cdot \left( l_{\text{total}} - \frac{b_{\text{sign}}}{2} \right) = 39.0 \cdot \text{kip} \cdot \text{ft}$$